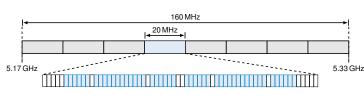


## Computer Networking and IT Security (INHN0012)

Tutorial 4

## Problem 1 Achievable data rates with IEEE 802.11a Wireless LAN

In this problem, we consider the physical layer of IEEE 802.11a (one of the WLAN standards). IEEE 802.11a carrier frequencies between 5127 MHz and 5910 MHz. Since the regulation of radio frequencies depends on the country, the available frequency ranges differ in international comparison. In Germany, for example, only the 5170 MHz to 5330 MHz range is available without restrictions. This corresponds to a bandwidth of 160 MHz, which is divided into a total of 8 channels of 20 MHz each. Each channel is in turn divided into 64 subcarriers of 312.5 kHz each (see Figure 1.1). Of these subcarriers, only 48 are used for data transmission<sup>1</sup>.



data rate [Mbit/s]	modulation	code rate
6	BPSK	1/2
9	BPSK	3/4
12	QPSK	1/2
18	QPSK	3/4
24	16-QAM	1/2
36	16-QAM	3/4
48	64-QAM	2/3
54	64-QAM	3/4

Figure 1.1: IEEE 802.11a channel distribution. Of the total of 64 subcarriers, only 48 (blue) are used for data transmission.

Figure 1.2: Data rates, modulation methods and code rates for IEEE 802.11a.

The symbol duration (temporal extension of a transmission pulse) is therefore 1/312.5 kHz =  $3.2 \mu$ s. To avoid interference from reflections, a guard interval ("Guard Interval") is inserted between symbols. The effective symbol duration is therefore  $T_s = 4 \mu$ s.

The effective data rate that can be achieved depends on the modulation method used and the code rate of the channel code. These are listed in Table 1.2.

## For the time being, we only consider the maximum transmission rate $r_{max} = 54 \text{ Mbit/s}$ .

a)\* How many bits are transmitted per symbol?

b) How many bits in total are transmitted per symbol duration when using 48 subcarriers?

c) The value calculated in Subproblem b) relates to channel words, i. e., redundancy is included. Determine the amount of user data transmitted per symbol duration.

d) Using the result from Subproblem c) confirm the maximum data rate  $r_{max} = 54 \text{ Mbit/s}$ .

e)\* Now, using Hartley's law, determine the minimum bandwidth  $B_{min}$  necessary to achieve a data rate of 54 Mbit/s using 64 distinguishable symbols.

f) \* Determine the minimum Shannon SNR in units of dB so that theoretically the maximum data rate  $r_{max} = 54 \text{ Mbit/s can be achieved.}$ 

**Hint:** For simplicity, assume the total channel bandwidth of B = 20 MHz.

g) The signal power at the receiver is now  $45 \mu$ W. The noise has a power of  $15 \mu$ W. Which modulation method and which code rate will be used under these conditions? **Hint:** For simplicity, assume the total channel bandwidth of *B* = 20 MHz.

<sup>&</sup>lt;sup>1</sup>The remaining subcarriers are either unused or are used for transmission of so-called pilot symbols, which are used for channel estimation. We disregard this in this problem

## Problem 2 Transmission Channels

A new undersea cable has connected Japan and the USA since 2010. The cable runs from Chikura near Tokyo to Los Angeles in California (approx. 10 000 km) and consists of 8 fiber pairs (in each fiber pair, one fiber is used for one direction and the other fiber for the other direction). The transmission rate amounts to a total of 7.68 Tbit/s per direction.

As a simplifying assumption, we assume that the light only travels the path of the cable and that no signal impairments or delays occur due to signal amplifiers, connectors and the like. The relative propagation speed of light within an optical fiber (as well as in copper cables) is approximately  $\nu = 2/3$  in relation to the speed of light in a vacuum  $c_0 = 3 \cdot 10^8$  m/s.

a)\* Determine the propagation delay from Chikura to Los Angeles within the cable.

b)\* What does the bandwidth delay product mean?

c) Determine the bandwidth delay product.

Laying and maintaining a submarine cable is very complex. The connection between the two cities could also be made via satellite. Take a brief look at the two connection paths in relation to the round trip time (RTT<sup>2</sup>).

Assume that the submarine cable is in direct airline connection between Chikura and Los Angeles. In doing so, neglect the curvature of the earth. A geostationary satellite (36 000 km altitude) is located exactly above the center of the route.

d) Determine the minimum RTT for the submarine cable. **Note:** Think about which component of the RTT makes the most significant contribution in this case.

e) Determine the minimum RTT for a corresponding satellite connection.

**Note:** Consider which sections of the route can be neglected if necessary. The curvature of the earth may be neglected.

<sup>&</sup>lt;sup>2</sup>RTT is the time it takes for a message to travel from the sender to the recipient and back again